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# Selection of a Suitable Material by a Multi-Criteria Decision Aid Method (MCDM) for the Manufacture of the Buckets of a Micro Pelton Turbine

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## Keywords

Evacuated Tube Solar Collector, Inertia of Water, Optimal flow control

### **ABSTRACT**

This article aims to investigate the effect of inertia on the outlet temperature of an evacuated tube solar collector. The experiments were conducted during a 24h period in Minquin County (latitude 38034'N, Longitude 10303'E). An analysis was made to determine whether the evacuated tube solar collectors' fluid thermal inertia impacts the water storage tank temperature. The results showed differences between the useful energy delivered to the water storage tank in the case with mass flow rate adjusted depending on the incident solar radiation for the entire two days in which experiments were conducted. Two days of cloud and sunshine were considered. An indirect optimal control technique refers to the impacts of the inertia of water on the outlet collector temperature, the on/off control of the pump, and the useful heat gain from the storage tank. During days with clear sky, the average solar radiation, mass flow rate, outlet, and tank temperature were 640.02W/ m<sup>2</sup>, 0.06kg/s, 29°C, and 44.24°C, respectively. For cloudy day was 449W/m<sup>2</sup>, 0.02kg/s, 27°C and 42°C respectively. The control system is provided to run the heating circulating pump after rest for several minutes to facilitate the exhaust system, then continues to run for a cycle. The  $D_{_{TP,\mathrm{OPF}}}$  and  $\ D_{_{TP,\mathrm{\,OFF}}}$  range from  $3^{0}\mathrm{C}$  to  $10^{0}\mathrm{C}$  and from  $0.2^{0}\mathrm{C}$  to  $1.5^{0}\mathrm{C},$ respectively.

#### INTRODUCTION

China has become the world's most extensive solar water heating system for production and applications. Moreover, automated control technology has advanced and improved significantly, making it feasible to handle even complex systems. Early approaches to energy gain maximization through mass flow rate control are reported in Refs. (Kovarik et al., 1976) and (Bejan et al., 1982). More recently, little work has been done to investigate the dynamic characteristics that affect the performance of the entire thermal systems, including heating, air conditioning, and control systems. Much research on the collector's thermal properties is concentrated on the steady-state or quasi-steady-state process [John et al.,1991, Han Zongwei et al., 2008]. For instance, the minimum cost per unit of energy transferred was considered (Horel et al.,1978), while in (Hollands et al., 1992), the amount of collected energy was maximized. Different optimal strategies were found when the exergy gain was analyzed (Bejan, 1982). More advanced approaches assume the controlled variable is the energy gain (to be maximized), the amount of collected energy (to be maximized), and the exergy gain (to be maximized) (Kovarik et al., 1976, Horel et al., 1978, Bejan et al., 1982, Hollands et al., 1992).

The optimal flow rate control in a solar collector under simplified weather conditions (assumed as sinusoidal time functions) was studied by (Saltiel et al., 1985). The optimal control of a closed-loop system based on a realistic solar collector model was analyzed using a sizeable meteorological database (Badescu, 2008). Two empirical control strategies have been proposed by (Furbo et al., 1996) for a solar domestic hot water system. The second method from (Furbo et al., 1996) has been slightly

changed recently in (Nhut et al., 2013), where simulations have been performed under South Korean latitudes and climates over a single spring day. In this paper, the heat-balanced equation for solving the collector temperature in the unsteady state was theoretically and experimentally developed, and a detailed study of the influence of water inertia on the solar heating system was presented. The main focus is on the all-glass evacuated tube solar collector and from the angle of the entire solar water heating system (including the control system), thoroughly studying the effect of water inertia on the outlet collector water temperature, the on/off control of pump and the heat gain.

### **METHODOLOGY**

The energy-balanced equation can describe the heat transfer process of solar collectors. In the steady state, the incident radiation on the collector surface is equal to the sum of heat and several different loss terms, as is evident from the energy balance of the absorber of a solar thermal collector, which is given by the following expression:

$$\frac{Q}{A_c} = \frac{mc_p(T_o - T_i)}{A_c} = F_R[(\tau \alpha)G_T - U_L(T_i - T_a)] \tag{1}$$

The collector efficiency calculate by integrating hour-step efficiency and is expressed as:

$$\eta = \frac{mc_p(T_o - T_i)}{A_c * G_T} = F_R(\tau \alpha) - F_R U_L \frac{(T_i - T_a)}{G_T}$$
 (2)

Where:

- Ac is Evacuated tube solar collector absorber area, m<sup>2</sup>
- GT is the global intensity of solar radiation, W/m²
- T<sub>0</sub> is outlet temperature, <sup>0</sup>C

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- T<sub>i</sub> is inlet temperature, <sup>0</sup>C
- Ta is ambient temperature, <sup>0</sup>C
- Ts is tank temperature, <sup>0</sup>C
- · Q is Useful energy gain, W
- m is the mass flow rate of fluid through the collector, kg/s
- C<sub>p</sub> is the Heat capacity of water, kJ/kg<sup>0</sup>C
- η is clean collector efficiency
- Fr is The collector heat removal factor
- *UL* is the heat coefficient between the water tank and the ambient temperature
  - T is the transmission coefficient of glazing
  - $\tau \alpha$  is the Absorptance-transmittance product

The condition of the controller to turn the pumps is when the value of solar energy delivered to the load exceeds the value of the energy needed to operate the pump [16]. Control systems are often used when the mass flow rate has two allowable values: maximum and zero. A solar radiant floor heating system was established to analyze the dynamic performance. It consists of a solar water heating system (including a pump control system, and the radiant floor heating system.

Pump P starts when the exit temperature from the solar collectors exceeds  $D_{\tiny TP,\,ON}$  the temperature Ts in the water storage tank. The pump P stops if To-Ts <  $D_{\tiny TP,\,OFE}$ 

$$Q_u = \begin{cases} 0 & (Pump \ P \ does \ not \ operate) \\ \frac{mc_p(T_0 - T_i)}{A_c} = F_R[(\tau \alpha)G_T - U_L(T_i - T_a)] & (Pump \ P \ operate) \end{cases}$$
(3)

$$Q_u = \left\{ \begin{array}{cc} {\rm To-Ts} \, < \, {\rm DT_{P,OFF}} & (\textit{Pump P does not operate}) \\ {\rm To-Ts} \, > \, {\rm DT_{P,ON}} & (\textit{Pump P operate}) \end{array} \right. \tag{4}$$

## System Description

The schematic of the experiment is shown in Figure. 1, and the technical specification is in table 1. The Evacuated Tube Solar Collector was experimentally investigated at Minquin County (latitude 38034'N, Longitude 10303'E). The typical control system has four heat coils with platinum resistance temperature sensors (pt100, manufactured by Beijing Sailing Technology Co., Ltd., with a precision of  $\pm 0.1$  °C) mounted on the ambient, inlet, outlet, and tank of the collector. The flow rate of hot water with an LWGY-15 turbine flow meter (manufactured by Shanghai Huaman Industrial Co., Ltd., with a precision of  $\pm 0.45\%$ ). The total solar radiation was recorded by Pyranometers (Kipp & Zonen CM11). Each measuring instrument connect to the computer via interfaces and is automatically scanned at 10s intervals and recorded by Agilent 349702

## Meteorological and Actinometric Data

The weather data was experimentally investigated at Minchin, China. The data was chosen for Sunny and Cloudy day. The performance of experiments was conducted for a whole day. Measurements were recorded every 10 seconds. The data obtained from the tests in the system are based on 16 and 27th December, 2014. Sunny day maximum value of ambient temperature and Solar radiation (Figure.1 and 2) was 14.37°C and 945.6W/m², respectively, while for the cloudy day was 8.1°C and 861.2 W/m², respectively.

Table 1: Technical specifications

Absorbing coating	Absorptivity [-] 0.94 Emissivity [-] 0.06
Outer glass envelope and absorber glass tube	Outer diameter of glass envelope [m] 0.058 Outer diameter of absorber tube [m] 0.047 Glass tube length [m] 1.56 Aperture width [m] 0.1105 Thickness of glass [m] 0.0016 Thermal conductivity of glass [W/(m K)] 1.2 Transmittance of glass [-] 0.92
Aluminum fin	Thickness [m] 0.0008 Thermal conductivity [W/(m K)] 220
Copper U-tube	Outer diameter [m] 0.0063 Thickness [m] 0.0005 Thermal conductivity [W/(m K)] 370
Header section	Outer diameter [m] 0.0063 Thickness [m] 0.0005 Thermal conductivity [W/(m K)] 370
Number of glass tubes	30

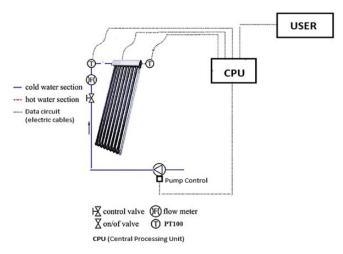


Figure 1: Experiment Control system

## **RESULTS**

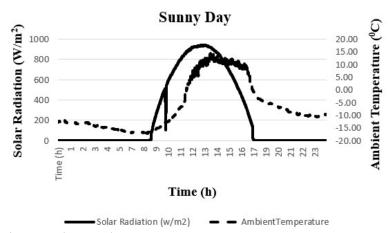


Figure 2: Solar Radiation on 16th December 2014

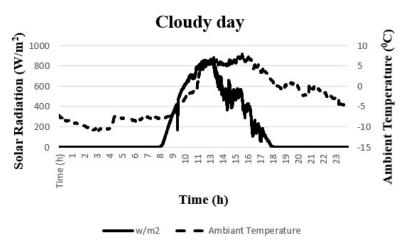


Figure 3: Solar Radiation on 27th December 2014

Table 2: Experiment results for Sunny day

	Solar Radiation (w/m²)	Outlet Temperature (°C)	Inlet Temperature (°C)	Tank temperature (°C)	Ambient Temperature (°C)	Mass Flowrate (kg/s)
min	0.11	11.00	13.66	35.81	-17.17	0.00
max	945.65	65.77	60.10	58.84	14.37	0.30
average	640.02	29.25	32.97	44.24	-6.43	0.06

Table 3:	Experiment	results for	Sunny day
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	Solar Radiation (w/m²)	Outlet Temperature (°C)	Inlet Temperature (°C)	Tank temperature (°C)	Ambient Temperature (°C)	Mass Flowrate (kg/s)
min	0.11	11.00	13.66	35.81	-17.17	0.00
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average	640.02	29.25	32.97	44.24	-6.43	0.06

#### **DISCUSSIONS**

After the outdoor temperature and the incident solar radiation have been specified, two sets of conditions of thermal inertia have been investigated for cloudy and Sunny days. The hourly variation of inlet, outlet (inertiaconsidered models), and Tank temperature. In literature(Knudsen, S, 2002), the control strategy and operation are as follows. Figure 4 (a,b) shows Pump P starts when the exit temperature from the solar collectors, To, exceeds by  $D_{TRON}$  the temperature Ts in the water storage tank. The pump P stops if To -Ts <  $D_{TROFF}$  Usual values of  $D_{TRON}$  and  $D_{TROFF}$  range from  $3^{\rm 0}{\rm C}$  to  $10^{\rm 0}{\rm C}$  and from  $0.2^{\rm 0}{\rm C}$  to  $1.5^{\rm 0}{\rm C}$ , respectively.

During the night, the pump at the collector side turned off, and the water in the collector was in thermal equilibrium. For a sunny day, the water temperature increased sharply without considering the inertia of the water, causing the pump to switch on at 17h00 and transfer heat to the storage tank, shown in Figure 4 (a). The difference between Tank and outlet temperature (D<sub>TPON</sub>>3 °C).

After 17:00, the solar radiation was unable to provide sufficient heat, which resulted in shutting down the pump at 23h00. The outlet and Tank temperature of the inertia model fell rapidly, then reduced slowly to its minimum. The difference between the Tank and outlet temperature (D<sub>TP,OF</sub>F<0.2°C) decreased until the night (23h00) turned, and the water in the collector was in thermal equilibrium. Sunshine duration was 9 hours and 21 Minutes, as shown in Figure 2. The average solar radiation intensity, mass flow rate, and ambient temperature were 248.1W/m², 0.06kg/s, and -6.4°C, respectively (table 2). The data analysis based on equation (3) provides heat to that day of 10311.96 kW.

For a cloudy day, the pump switched on at 17h00 and transferred heat to the storage tank, shown in Figure 5 (b). Because of that day, the solar radiation was low to provide sufficient heat, the pump shut down the pump at 21h03, and the water in the collector was in thermal equilibrium. Solar heating is shown on a cloudy day for a heating cycle and a return flow temperature curve

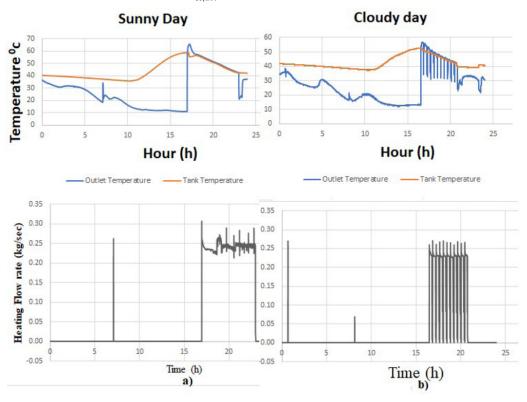


Figure 4: Optimal control of the inertia on 16 and 27th December 2014 Optimal control of the inertia on 16 and 27th December 2014



over time. The control system is provided to run the heating circulating pump and rest for several minutes to facilitate the exhaust system, then continues to run for a cycle. Sunshine duration was 9 hours 34 Minutes, as shown in Figure 3, the average solar radiation intensity and ambient temperature were 449W/m², 0.02kg/s, and -3°C, respectively (table 3). The heat provided that day was 7641.192 kW.

#### **CONCLUSION**

Conventional models should have considered the influence of the inertia of water in the collectors, which would result in incomprehensive recognition of the dynamic characteristic of collectors, thus affecting the objective assessment of the entire thermal system. For all-glass evacuated tube solar collectors, increasing pump turnon time, the inertia of water decrease, and lost heat gain from the storage tank, whereas the pump will be on/off more frequently. For a sunny day, the difference between Tank and outlet temperature (D<sub>TPON</sub> >3°C) and (D<sub>TPOFF</sub> <0.2°C). After 17:00, the solar radiation was unable to provide sufficient heat, which resulted in shutting down the pump at 23h00. The outlet and Tank temperature of the inertia model fell rapidly, then reduced slowly to its minimum. For cloudy, the difference between  $D_{TPON}$ and  $D_{\text{TP,OFF}}$  is the same. But that day, the solar radiation was low to provide sufficient heat, the pump shut down the pump at 21h03, and the water in the collector was in thermal equilibrium.

Reducing water inertia will increase pump turn-on time and heat gain depending on meteoritical conditions. This research will help relevant experts to evaluate the solar energy system more accurately, and the existing will improve solar energy, simulation models.

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$$r_{ij} = \frac{X_{ij}}{\sqrt{\sum_{i=1}^{i=m} x_{ij}^2}}$$
Where  $i=1, 2, 3, ..., m$  and  $j=1, 2, 3, ..., n$ 

$$S_{j} = \sum_{i=1}^{n} w_{i} (f_{i}^{*} - f_{ij}) / (f_{i}^{*} - f_{i}^{-})$$

$$R_{j} = \max_{i} [(f_{i}^{*} - f_{ij}) / (f_{i}^{*} - f_{i}^{-})]$$
18

$$Q_{j} = \vartheta \frac{(s_{j} - s^{*})}{(s^{-} - s^{*})} + (1 - \vartheta) \frac{(R_{j} - R^{*})}{(R^{-} - R^{*})}$$
19

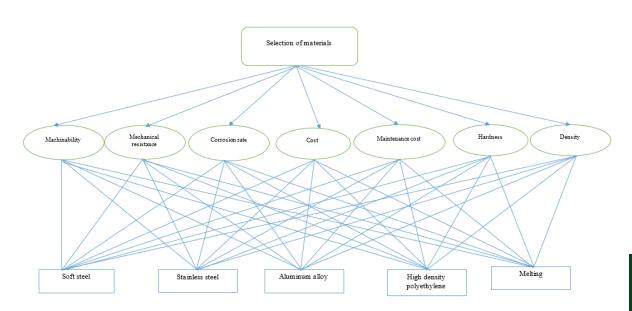


Figure 2: The decision-making hierarchy by the AHP.



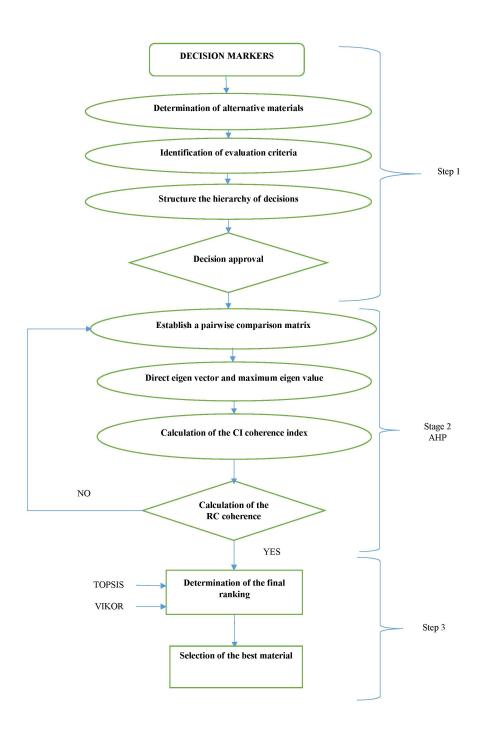


Figure 3: Schematic flow chart of developed methodology for optimal material selection



Table 3: The pairwise comparison matrix developed using the AHP method for the seven (7) criteria.

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	Machinability	Corrosion	Density	Tensile strength	Hardness	Cost (€	Maintenance
		resistance	(kg/cm3)	Rm (Mpa)		/ kilo)	cost
M	1.0000	7.0000	3.0000	4.0000	3.0000	4.0000	2.0000
UTS	0.1429	1.0000	0.3333	0.5000	0.3333	0.2000	0.5000
D	0.3333	3.0000	1.0000	3.0000	3.0000	2.0000	5.0000
RC	0.2500	2.0000	0.3333	1.0000	0.3333	0.3333	0.5000
Н	0.3333	3.0000	0.3333	3.0000	1.0000	3.0000	3.0000
RC	0.2500	5.0000	0.5000	3.0000	0.3333	1.0000	2.0000
CM	0.5000	2.0000	0.2000	2.0000	0.3333	0.5000	1.0000
TOTAL	2.8095	23.0000	5.7000	16.5000	8.3333	11.0333	14.0000

We used equation (2) for matrix normalization.

**Table 4:** Normalization of the expanded pairwise comparison matrix.

Criteres	M	Uts	D	Cr	Н	Cr	Cm
M	0,32777357	0,27694945	0,64489173	0,22911482	0,46952812	0,48537338	0,16513379
UTS	0,0468	0,0396	0,0717	0,0286	0,0522	0,0243	0,0413
D	0,1093	0,1187	0,2150	0,1718	0,4695	0,0589	0,4128
CR	0,0819	0,07912842	0,0717	0,0573	0,0522	0,0404	0,0413
Н	0,1093	0,11869262	0,0717	0,1718	0,1565	0,3640	0,2477
CR	0,0819	0,19782104	0,1075	0,1718	0,0522	0,1213	0,1651
CM	0,1639	0,07912842	0,0430	0,1146	0,0522	0,0607	0,0826
TOTAL	0,9209	0,9100	1,2253	0,9451	1,3042	1,1550	1,1559

To determine the consistency analysis of the pairwise comparison matrix, equations (3), (5), and (6) are used. Thus Table 5 presents the result obtained with the AHP method.

**Table 5:** The result obtained by the AHP method.

Table 5. The re	Suit Obtained by the Mill 1	neurou.		
Criteria	Weight	λ_max	CI	CR
M	0.32777357	7.54269427	0.09044904	0.06699929
UTS	0.03956421			
L	0.21496391			
D	0.0572787			
VS	0.15650937			
RC	0.12134335			
CM	0.08256689			

After determining the weight of the criteria with the AHP, we will apply the TOPSIS technique to rank the selected alternatives. Thus Table 6 shows the vector matrix.

**Table 6:** Vector matrix of chosen materials

Materials/		Properties	Properties					
Alternatives	Machinability	Corrosion resistance		Tensile strength (Mpa)		Cost (€/kilo)	Maintenance cost	
Soft steel	3	1	7.85	400	5	1.25	4	
Stainless steel	4	4	7.7	720	4	1.5	3	
HDPE	5	5	0.965	6	2	1.67	2	
high density								
polyethylene								
Melting	3	2	7.2	350	4	0.9	4	
Aluminum alloy	4	5	2.7	80	4	2.48	2	



**Table 7:** The standardized decision matrix with criteria and alternatives.

Criteria	Machinability	Corrosion	Density	Tensile	Hardness	Cost	Maintenance
Alternatives		resistance		strength		(price)	cost
Soft steel	0.043478261	0.01408451	0.06171324	0.000617536	0.0877193	0.09434461	0.10810811
Stainless steel	0.057971014	0.05633803	0.06053401	0.001111564	0.07017544	0.11321353	0.08108108
HDPE	0.072463768	0.07042254	0.0075864	9.26303E-06	0.03508772	0.12604439	0.05405405
Melting	0.043478261	0.02816901	0.05660323	0.000540344	0.07017544	0.06792812	0.10810811
Aluminum	0.057971014	0.07042254	0.02122621	0.000123507	0.07017544	0.1871797	0.05405405
alloy							

Table 8: The weighted normalized decision matrix with criteria and alternatives

Criteria	Machinability	Corrosion	Density	Tensile	Hardness	Cost	Maintenance
Alternatives	•	resistance		strength		(price)	cost
Soft steel	0.014251025	0.00055724	0.01326612	3.53716E-05	0.01372889	0.01144809	0.00892615
Stainless steel	0.019001366	0.00222897	0.01301263	6.36689E-05	0.01098311	0.01373771	0.00669461
HDPE	0.023751708	0.00278621	0.0016308	5.30575E-07	0.00549156	0.01529465	0.00446308
Melting	0.014251025	0.00111448	0.01216765	3.09502E-05	0.01098311	0.00824262	0.00892615
Aluminum	0.019001366	0.00278621	0.00456287	7.07433E-06	0.01098311	0.02271301	0.00446308
alloy							
Weight	0.327773567	0.03956421	0.21496391	0.057278704	0.15650937	0.12134335	0.08256689

Table 9: The calculation of the best ideal value and the worst ideal value

V+	0.023751708	0.00278621	0.0016308	6.36689E-05	0.00549156	0.02271301	0.00892615
V-	0.014251025	0.00055724	0.01326612	5.30575E-07	0.01372889	0.00824262	0.00446308

**Table 10:** The Euclidean distance () best ideal () worst ideal and the performance score used for ranking S. + S.

Table 10. The Eden	deall distallee of best ideal of	voist ideal and the periorni	affect score used for ra	ilkiiigo <sub>i</sub> o <sub>i</sub>
Alternatives	$S_i^+$	$S_i^-$	Pi	Rank
Soft steel	0.020624374	0.00549502	0.21038089	4
Stainless steel	0.016374223	0.00825492	0.33516871	3
HDPE	0.008657663	0.01866003	0.68307485	1
Melting	0.021062601	0.00538297	0.20354916	5
Aluminum alloy	0.009013445	0.01789447	0.66502624	2

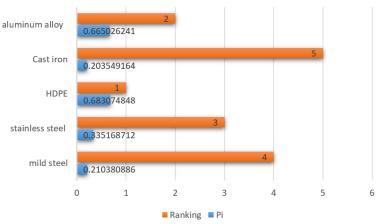


Figure 4: Classification diagram TOPSIS method



Table 11: The standardized decision matrix

Criteria	Machinability	Corrosion	Density	Tensile	Hardness	Cost	Maintenance	
		resistance		strength		(price)	cost	
Soft steel	0.04347826	0.01408451	0.06171324	0.00061754	0.0877193	0.09434461	0.10810811	
Stainless steel	0.05797101	0.05633803	0.06053401	0.00111156	0.07017544	0.11321353	0.08108108	
HDPE	0.07246377	0.07042254	0.0075864	9,263E-06	0.03508772	0.12604439	0.05405405	
Melting	0.04347826	0.02816901	0.05660323	0.00054034	0.07017544	0.06792812	0.10810811	
Aluminum	0.05797101	0.07042254	0.02122621	0.00012351	0.07017544	0.1871797	0.05405405	
alloy								

The best and worst values for each criterion are calculated using Equation 17 and the resulting values are tabulated in Table 12.

Table 12: The best and the worst values of each criterion

X+	Best	5.0000	5.0000	7.8500	720.0000	5.0000	2.4800	4.0000
X-	worth	3.0000	1.0000	0.9650	6.0000	2.0000	0.9000	2.0000

Table 13: Result of the classification by the VIKOR method

Criteria	Machi	Corrosion	Density	Tensile	Hard-	Cost	Mainte-	Si	Ri	Qi	rank
	-nability	resistance		strength	ness	(price)	nance cost				
Soft steel	0.81230841	0.04931595	0.24316639	0.05775999	0.25627266	0.18321735	0.16067071	1.76271144	0.81230841	0.52072945	4
Stain lesssteel	0.80993323	0.04889802	0.2432032	0.05775999	0.25718791	0.18176822	0.16178648	1.76053706	0.80993323	0.26275352	3
HDPE	0.80755806	0.04875871	0.24485634	0.05775999	0.25901843	0.18078282	0.16290225	1.7616366	0.80755806	0.01678676	1
Melting	0.81230841	0.04917664	0.37101953	0.05775999	0.25718791	0.18524612	0.16067071	1.89336931	0.81230841	1	5
Aluminum alloy	0.80993323	0.04875871	0.24443048	0.05775999	0.25718791	0.17608765	0.16290225	1.75706022	0.80993323	0.25	2
							S*,R*	1.75706022	0.80755806		
							S-,R-	1.89336931	0.81230841		

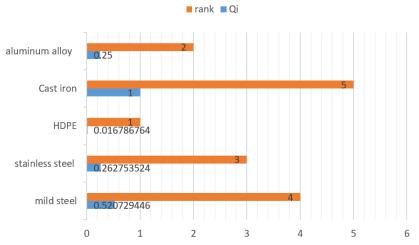


Figure 5: Classification diagram VIKOR method









